

Lewannick Primary School

How we teach calculations:

Calculation Policy for Mathematics

September 2014

What you need to know about calculations

Mathematics will be at the core of your child's schooling from the moment they start to the moment they leave. They will be involved in drawing, measuring, handling data and lots of other practical activities that will help your child to understand and enjoy the subject. This booklet offers guidance to the methods used to help our pupils with calculations. The methods we are advocating are in line with the new National Curriculum (from September 2014). We hope this will be helpful to you and that you will be able to support your child in learning by heart the basic rules which will assist in mental recall e.g. number bonds and multiplication tables.

The methods that we use in school may or may not be familiar to you. Children are often confused when they ask parents for help at home and they try to teach the methods that they themselves were taught. Knowing how the methods in this booklet work will help you to help your children.

All staff in school work from this document so that we can ensure the consistency of our approach and can make sure that the children move onto the next step when they are ready.

The four operations that are covered by this booklet are addition, subtraction, multiplication and division. Whichever operation is being taught the child needs to experience all of these steps to completely conquer it.

- 1) using objects
- 2) using pictures
- 3) using a numberline
- 4) using an expanded method
- 5) using a compact written method

Mental methods first

Children should always be encouraged to consider if a mental calculation would be appropriate before using written methods. These are covered in the first part of each section.

Why do children need to do written calculations?

- To represent work that has been done practically.
- To support, record and explain mental calculation
- To keep track of steps in a longer task
- To work out calculations that are too difficult to do mentally

Children should be taught when it is appropriate to do an approximate or estimate first and should check with the inverse operation at the end.

By upper Key Stage 2, children should be confident in choosing and using a strategy that they know will get them to the correct answer as efficiently as possible.

What can parents do to help?

- Count with their child
- Play number games
- Involve children when taking measurements or weighing items
- Take note of numbers in real life e.g. telephone numbers, bus numbers, lottery numbers etc.
- Give children opportunities to use money to shop, check change etc.
- Talking about the mathematics in football e.g. 'How many points does your favourite team need to catch the next team in the league?'
- When helping their children calculate use the method that they have been taught

Please don't...

- Teach your children that to multiply by 10 you 'just add a zero'. – you 'move the digits to the left and add a zero as a place holder'
- Tell them that you can move the decimal point. – You can't. You can only move the digits to the left or to the right
- Tell them that they are doing 'sums' – 'sum' is a mathematical word that means 'addition', everything else is a 'calculation'

Glossary

2-digit – a number with 2 digits like 23, 45, 12 or 60

3-digit – a number with 3 digits like 123, 542, 903 or 561

Addition facts – knowing that $1+1 = 2$ and $1+3 = 4$ and $2+5 = 7$. Normally we only talk about number facts with totals of 20 and under.

Array—An array is an arrangement of a set of numbers or objects in rows and columns –it is mostly used to show how you can group objects for repeated addition or subtraction.

Bridge to ten – a strategy when using numberlines. Adding a number that takes you to the next ‘tens’ number.

Bus Stop Method - traditional method for division with a single digit divisor

Concrete apparatus – objects to help children count – these are most often cubes (multilink) but can be anything they can hold and move.

Dienes (purple hundreds, tens and units blocks), Numicon, Cuisenaire rods are also referred to as **concrete apparatus**.

Column chunking – method of division involving taking chunks or groups or the divisor away from the larger number

Decimal number – a number with a decimal point

Divisor – the smaller number in a division calculation. The number in each group for chunking.

Double – multiply a number by 2

Exchanging – Moving a ‘ten’ or a ‘hundred’ from its column into the next column and splitting it up into ten ‘ones’ (or ‘units’) or ten ‘tens’ and putting it into a different column

Expanded Multiplication – a method for multiplication where each stage is written down and then added up at the end in a column

Find the difference – A method for subtraction involving counting up from the smaller to the larger number

Grid method – a method for multiplying two numbers together involving partitioning

Half - a number, shape or quantity divided into 2 equal parts

Halve – divide a number by 2

Integer - a number with no decimal point

Inverse – the opposite operation. Addition is the inverse of subtraction, multiplication is the inverse of division

Long Multiplication – column multiplication where only the significant figures are noted

Number bonds to ten – 2 numbers that add together to make ten, like 2 and 8, or 6 and 4.

Numberline – a line either with numbers or without (a blank numberline). Children use this tool to help them count on for addition of subtraction and also in multiplication and division.

Numberline Chunking - method of division involving taking chunks or groups or the divisor away from the larger number

Number sentence – writing out a calculation with just the numbers in a line E.G. $2+4=6$ or $35 \div 7 = 5$ or $12 \times 3 = 36$ or $32 - 5 = 27$

Partition – split up a larger number into the hundreds, tens and units. E.G. $342 - 300$ and 40 and 2

Place Value – knowing that in the number 342 – the ‘3’ means ‘3 hundreds’, the ‘4’ means ‘4 tens’ and the ‘2’ means ‘2’.

Quarter - a number, shape or quantity divided into 4 equal parts

Recombine – for addition, once you have partitioned numbers into hundreds, tens and units then you have to add then hundreds together, then add the tens to that total, then add the units to that total

Remainder – a whole number left over after a division calculation

Repeated addition – repeatedly adding groups of the same size for multiplication

Significant digit – the digit in a number with the largest value. E.G in 34 – the most significant digit is the 3, as it has a value of ‘30’ and the ‘4’ only has a value of ‘4’

Single digit – a number with only one digit. These are always less than 10.

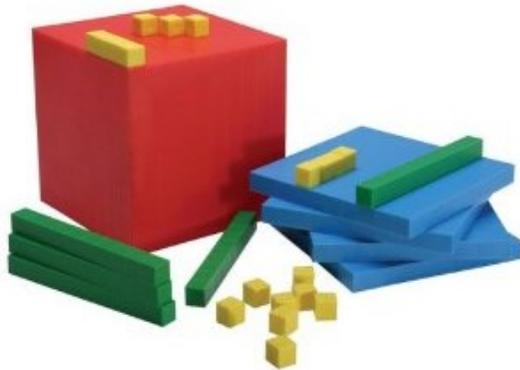
Taking away – a method for subtraction involving counting backwards from the larger to the smaller number

Tens number - a number in the ten times tables – 10,20,30,40 50,etc.

Unit – another term for single digit numbers. The right hand column in column methods is the ‘units’ column

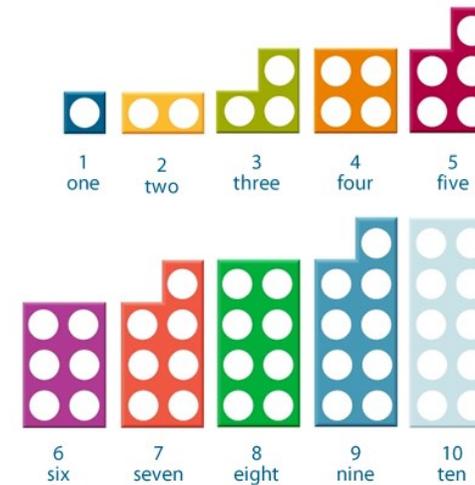
Some of the resources that your children will use to help with calculation

Dienes



Dienes, although it has been used in schools for years is a crucial step in knowing what a 'one' (unit), a ten, a hundred and a thousand look like and how they can be added together and split up to form smaller and larger numbers.

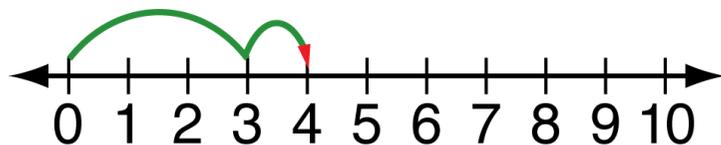
Numicon



Numicon is an especially useful resource as it can be used for teaching all four operations as well as fractions, decimals, percentages and a range of other aspects of maths. Each piece represents an integer from 1 to 10. The children love using it as it is colourful and tactile.

Numberlines

$$3 + 1 = 4$$



Numberlines are a mainstay of teaching calculations.

Number square

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

Bead string



KEY STAGE 1

Children in Years 1 and 2 will be given a really solid foundation in the basic building blocks of mental and written arithmetic. Through being taught place value, children will develop an understanding of how numbers work, so that they are confident with 2-digit numbers and beginning to read and say numbers above 100.

Addition and Subtraction: A focus on number bonds, first via practical hands-on experiences and subsequently using memorisation techniques, enables a good grounding in these crucial facts, and ensures that all children leave Year 2 knowing the pairs of numbers which make all the numbers up to 10 at least. Children will also have experienced and been taught pairs to 20. Children’s knowledge of number facts enables them to add several 1-digit numbers, and to add/subtract a 1-digit number to/from a 2-digit number. Another important conceptual tool is the ability to add/subtract 1 or 10, and to understand which digit changes and why. This understanding is extended to enable children to add and subtract multiples of 10 to and from any 2-digit number. The most important application of this knowledge is the ability to add or subtract any pair of 2-digit numbers by counting on or back in 10s and 1s. Children may extend this to adding by partitioning numbers into 10s and 1s.

Multiplication and Division: Children will be taught to count in 2s, 3s, 5s and 10s, and will relate this skill to repeated addition. Children will meet and begin to learn the associated $\times 2$, $\times 3$, $\times 5$ and $\times 10$ tables. Engaging in a practical way with the concept of repeated addition and the use of arrays enables children to develop a preliminary understanding of multiplication, and asking them to consider how many groups of a given number make a total will introduce them to the idea of division. Children will also be taught to double and halve numbers, and will thus experience scaling up or down as a further aspect of multiplication and division.

Fractions: Fractions will be introduced as numbers and as operators, specifically in relation to halves, quarters and thirds.

Year 1

	Mental calculation	Written calculation	Default for ALL children
Y1 +	Number bonds ('story' of 5, 6, 7, 8, 9 and 10) Count on in 1s from a given 2-digit number Add two 1-digit numbers Add three 1-digit numbers, spotting doubles or pairs to 10 Count on in 10s from any given 2-digit number Add ten to any 2-digit number Add 10 to any given 2-digit number Use number facts to add 1-digit numbers to 2-digit numbers <i>E.g. use $4 + 3$ to work out $24 + 3$, $34 + 3$</i> Add by putting the larger number first		Pairs with a total of 10 Count in 1s Count in 10s Count on 1 from any given 2-digit number

Y1 -	Number bonds ('story' of 5, 6, 7, 8, 9 and 10) Count back in 1s from a given 2-digit number Subtract one 1-digit number from another Count back in 10s from any given 2-digit number Subtract 10 from any given 2-digit number Use number facts to subtract 1-digit numbers from 2-digit numbers e.g. Use $7 - 2$ to work out $27 - 2$, $37 - 2$		Pairs with a total of 10 Count back in 1s from 20 to 0 Count back in 10s from 100 to 0 Count back 1 from any given 2-digit number
Y1 x	Begin to count in 2s, 5s and 10s Begin to say what three 5s are by counting in 5s, or what four 2s are by counting in 2s, etc. Double numbers to 10		Begin to count in 2s and 10s Double numbers to 5 using fingers
Y1 ÷	Begin to count in 2s, 5s and 10s Find half of even numbers to 12 and know it is hard to halve odd numbers Find half of even numbers by sharing Begin to use visual and concrete arrays or 'sets of' to find how many sets of a small number make a larger number		Begin to count in 2s and 10s Find half of even numbers by sharing

Year 2			
	Mental calculation	Written calculation	Default for ALL children
Y2 +	Number bonds – know all the pairs of numbers which make all the numbers to 12, and pairs with a total of 20 Count on in 1s and 10s from any given 2-digit number Add two or three 1-digit numbers Add a 1-digit number to any 2-digit number using number facts, including bridging multiples of 10 e.g. $45 + 4$ e.g. $38 + 7$ Add 10 and small multiples of 10 to any given 2-digit number Add any pair of 2-digit numbers		Know pairs of numbers which make each total up to 10 Add two 1-digit numbers Add a 1-digit number to a 2-digit number by counting on in 1s Add 10 and small multiples of 10 to a 2-digit number by counting on in 10s

<p>Y2 –</p>	<p>Number bonds – know all the pairs of numbers which make all the numbers to 12 Count back in 1s and 10s from any given 2-digit number Subtract a 1-digit number from any 2-digit number using number facts, including bridging multiples of 10 e.g. $56 - 3$ e.g. $53 - 5$ Subtract 10 and small multiples of 10 from any given 2-digit number Subtract any pair of 2-digit numbers by counting back in 10s and 1s or by counting up</p>		<p>Know pairs of numbers which make each total up to 10 Subtract a 1-digit number from a 2-digit number by counting back in 1s Subtract 10 and small multiples of 10 from a 2-digit number by counting back in 10s</p>
<p>Y2 ×</p>	<p>Count in 2s, 5s and 10s Begin to count in 3s Begin to understand that multiplication is repeated addition and to use arrays e.g. 3×4 is <i>three rows of 4 dots</i> Begin to learn the $\times 2$, $\times 3$, $\times 5$ and $\times 10$ tables, seeing these as 'lots of' e.g. <i>5 lots of 2, 6 lots of 2, 7 lots of 2</i> Double numbers up to 20 Begin to double multiples of 5 to 100 Begin to double 2-digit numbers less than 50 with 1s digits of 1, 2, 3, 4 or 5</p>		<p>Count in 2s, 5s and 10s Begin to use and understand simple arrays e.g. 2×4 is <i>two lots of four</i> Double numbers up to 10 Double multiples of 10 to 50</p>
<p>Y2 ÷</p>	<p>Count in 2s, 5s and 10s Begin to count in 3s Using fingers, say where a given number is in the 2s, 5s or 10s count e.g. <i>8 is the fourth number when I count in 2s</i> Relate division to grouping e.g. <i>How many groups of 5 in 15?</i> Halve numbers to 20 Begin to halve numbers to 40 and multiples of 10 to 100 Find $\frac{1}{2}$, $\frac{1}{3}$, $\frac{1}{4}$ and $\frac{3}{4}$ of a quantity of objects and of amounts (whole number answers)</p>		<p>Count in 2s, 5s and 10s Say how many rows in a given array e.g. <i>How many rows of 5 are in an array of 3×5?</i> Halve numbers to 12 Find $\frac{1}{2}$ of amounts</p>

LOWER KEY STAGE 2

In Lower Key Stage 2, children build on the concrete and conceptual understandings they have gained in Key Stage 1 to develop a real mathematical understanding of the four operations, in particular developing arithmetical competence in relation to larger numbers.

Addition and subtraction: Children are taught to use place value and number facts to add and subtract numbers mentally and they will develop a range of strategies to enable them to discard the 'counting in 1s' or fingers-based methods of Key Stage 1. In particular, children will learn to add and subtract multiples and near multiples of 10, 100 and 1000, and will become fluent in complementary addition as an accurate means of achieving fast and accurate answers to 3-digit subtractions. Standard written methods for adding larger numbers are taught, learned and consolidated, and written column subtraction is also introduced.

Multiplication and division: This key stage is also the period during which all the multiplication and division facts are thoroughly memorised, including all facts up to 12×12 . Efficient written methods for multiplying or dividing a 2-digit or 3-digit number by a 1-digit number are taught, as are mental strategies for multiplication or division with large but 'friendly' numbers, e.g. when dividing by 5 or multiplying by 20.

Fractions and decimals: Children will develop their understanding of fractions, learning to reduce a fraction to its simplest form, as well as finding non-unit fractions of amounts and quantities. The concept of a decimal number is introduced and children consolidate a firm understanding of 1-place decimals, multiplying and dividing whole numbers by 10 and 100.

Year 3

	Mental calculation	Written calculation	Default for ALL children
Y3 +	<p>Know pairs with each total to 20 e.g. $2 + 6 = 8$, $12 + 6 = 18$, $7 + 8 = 15$</p> <p>Know pairs of multiples of 10 with a total of 100</p> <p>Add any two 2-digit numbers by counting on in 10s and 1s or by using partitioning</p> <p>Add multiples and near multiples of 10 and 100</p> <p>Perform place-value additions without a struggle e.g. $300 + 8 + 50 = 358$</p> <p>Use place value and number facts to add a 1-digit or 2-digit number to a 3-digit number e.g. $104 + 56$ is 160 since $104 + 50 = 154$ and $6 + 4 = 10$ $676 + 8$ is 684 since $8 = 4 + 4$ and $76 + 4 + 4 = 84$</p> <p>Add pairs of 'friendly' 3-digit numbers e.g. $320 + 450$</p> <p>Begin to add amounts of money using partitioning</p>	<p>Use expanded column addition to add two or three 3-digit numbers or three 2-digit numbers</p> <p>Begin to use compact column addition to add numbers with 3 digits</p> <p>Begin to add like fractions e.g. $\frac{3}{8} + \frac{1}{8} + \frac{1}{8}$</p> <p>Recognise fractions that add to 1 e.g. $\frac{1}{4} + \frac{3}{4}$ e.g. $\frac{3}{5} + \frac{2}{5}$</p>	<p>Know pairs of numbers which make each total up to 10, and which total 20</p> <p>Add two 2-digit numbers by counting on in 10s and 1s e.g. $56 + 35$ is $56 + 30$ and then add the 5</p> <p>Understand simple place-value additions e.g. $200 + 40 + 5 = 245$</p> <p>Use place value to add multiples of 10 or 100</p>

<p>Y3 —</p>	<p>Know pairs with each total to 20 e.g. $8 - 2 = 6$ e.g. $18 - 6 = 12$ e.g. $15 - 8 = 7$</p> <p>Subtract any two 2-digit numbers Perform place-value subtractions without a struggle e.g. $536 - 30 = 506$</p> <p>Subtract 2-digit numbers from numbers > 100 by counting up e.g. <i>143 - 76 is done by starting at 76. Then add 4 (80), then add 20 (100), then add 43, making the difference a total of 67</i></p> <p>Subtract multiples and near multiples of 10 and 100 Subtract, when appropriate, by counting back or taking away, using place value and number facts Find change from £1, £5 and £10</p>	<p>Use counting up as an informal written strategy for subtracting pairs of 3-digit numbers e.g. $423 - 357$</p> <p>Begin to subtract like fractions e.g. $\frac{7}{8} - \frac{3}{8}$</p>	<p>Know pairs of numbers which make each total up to 10, and which total 20 Count up to subtract 2-digit numbers e.g. $72 - 47$</p> <p>Subtract multiples of 5 from 100 by counting up e.g. $100 - 35$</p> <p>Subtract multiples of 10 and 100</p>
<p>Y3 ×</p>	<p>Know by heart all the multiplication facts in the $\times 2$, $\times 3$, $\times 4$, $\times 5$, $\times 8$ and $\times 10$ tables Multiply whole numbers by 10 and 100 Recognise that multiplication is commutative Use place value and number facts in mental multiplication e.g. 30×5 is 15×10</p> <p>Partition teen numbers to multiply by a 1-digit number e.g. 3×14 as 3×10 and 3×4</p> <p>Double numbers up to 50</p>	<p>Use partitioning (grid multiplication) to multiply 2-digit and 3-digit numbers by 'friendly' 1-digit numbers</p>	<p>Know by heart the $\times 2$, $\times 3$, $\times 5$ and $\times 10$ tables Double given tables facts to get others Double numbers up to 25 and multiples of 5 to 50</p>
<p>Y3 ÷</p>	<p>Know by heart all the division facts derived from the $\times 2$, $\times 3$, $\times 4$, $\times 5$, $\times 8$ and $\times 10$ tables Divide whole numbers by 10 or 100 to give whole number answers Recognise that division is not commutative Use place value and number facts in mental division e.g. $84 \div 4$ is half of 42</p> <p>Divide larger numbers mentally by subtracting the 10th multiple as appropriate, including those with remainders e.g. $57 \div 3$ is $10 + 9$ as $10 \times 3 = 30$ and $9 \times 3 = 27$</p> <p>Halve even numbers to 100, halve odd numbers to 20</p>	<p>Perform divisions just above the 10th multiple using horizontal or vertical jottings and understanding how to give a remainder as a whole number Find unit fractions of quantities and begin to find non-unit fractions of quantities</p>	<p>Know by heart the division facts derived from the $\times 2$, $\times 3$, $\times 5$ and $\times 10$ tables Halve even numbers up to 50 and multiples of 10 to 100 Perform divisions within the tables including those with remainders e.g. $38 \div 5$</p>

Year 4

	Mental calculation	Written calculation	Default for ALL children
Y4 +	<p>Add any two 2-digit numbers by partitioning or counting on Know by heart/quickly derive number bonds to 100 and to £1 Add to the next 100, £1 and whole number e.g. $234 + 66 = 300$ e.g. $3 \cdot 4 + 0 \cdot 6 = 4$</p> <p>Perform place-value additions without a struggle e.g. $300 + 8 + 50 + 4000 = 4358$</p> <p>Add multiples and near multiples of 10, 100 and 1000 Add £1, 10p, 1p to amounts of money Use place value and number facts to add 1-, 2-, 3- and 4-digit numbers where a mental calculation is appropriate e.g. $4004 + 156$ by knowing that $6 + 4 = 10$ and that $4004 + 150 = 4154$ so the total is 4160</p>	<p>Column addition for 3-digit and 4-digit numbers e.g.</p> $\begin{array}{r} 5347 \\ 2286 \\ + 1495 \\ \hline 121 \\ \hline 9128 \end{array}$ <p>Add like fractions e.g. $\frac{3}{5} + \frac{4}{5} = \frac{7}{5} = 1 \frac{2}{5}$</p> <p>Be confident with fractions that add to 1 and fraction complements to 1 e.g. $\frac{2}{3} + _ = 1$</p>	<p>Add any 2-digit numbers by partitioning or counting on Number bonds to 20 Know pairs of multiples of 10 with a total of 100 Add 'friendly' larger numbers using knowledge of place value and number facts Use expanded column addition to add 3-digit numbers</p>
Y4 -	<p>Subtract any two 2-digit numbers Know by heart/quickly derive number bonds to 100 Perform place-value subtractions without a struggle e.g. $4736 - 706 = 4030$</p> <p>Subtract multiples and near multiples of 10, 100, 1000, £1 and 10p Subtract multiples of 0.1 Subtract by counting up e.g. $503 - 368$ is done by adding $368 + 2 + 30 + 100 + 3$ (so we added 135)</p> <p>Subtract, when appropriate, by counting back or taking away, using place value and number facts Subtract £1, 10p, 1p from amounts of money Find change from £10, £20 and £50</p>	<p>Use expanded column subtraction for 3- and 4-digit numbers Use complementary addition to subtract amounts of money, and for subtractions where the larger number is a near multiple of 1000 or 100 e.g. $2002 - 1865$</p> <p>Subtract like fractions e.g. $\frac{4}{5} - \frac{3}{5} = \frac{1}{5}$</p> <p>Use fractions that add to 1 to find fraction complements to 1 e.g. $1 - \frac{2}{3} = \frac{1}{3}$</p>	<p>Use counting up with confidence to solve most subtractions, including finding complements to multiples of 100 e.g. $512 - 287$ e.g. $67 + _ = 100$</p>

<p>Y4 ×</p>	<p>Know by heart all the multiplication facts up to 12×12 Recognise factors up to 12 of 2-digit numbers Multiply whole numbers and 1-place decimals by 10, 100, 1000 Multiply multiples of 10, 100 and 1000 by 1-digit numbers e.g. 300×6 e.g. 4000×8 Use understanding of place value and number facts in mental multiplication e.g. 36×5 is half of 36×10 e.g. $50 \times 60 = 3000$ Partition 2-digit numbers to multiply by a 1-digit number mentally e.g. 4×24 as 4×20 and 4×4 Multiply near multiples by rounding e.g. 33×19 as $(33 \times 20) - 33$ Find doubles to double 100 and beyond using partitioning Begin to double amounts of money e.g. $\pounds 35.60$ doubled is $\pounds 71.20$</p>	<p>Use a vertical written method to multiply a 1-digit number by a 3-digit number (ladder method) Use an efficient written method to multiply a 2-digit number by a number between 10 and 20 by partitioning (grid method)</p>	<p>Know by heart multiplication tables up to 10×10 Multiply whole numbers by 10 and 100 Use the grid method to multiply a 2-digit or a 3-digit number by a number ≤ 6</p>
<p>Y4 ÷</p>	<p>Know by heart all the division facts up to $144 \div 12$ Divide whole numbers by 10, 100, to give whole number answers or answers with 1 decimal place Divide multiples of 100 by 1-digit numbers using division facts e.g. $3200 \div 8 = 400$ Use place value and number facts in mental division e.g. $245 \div 20$ is half of $245 \div 10$ Divide larger numbers mentally by subtracting the 10th or 20th multiple as appropriate e.g. $156 \div 6$ is $20 + 6$ as $20 \times 6 = 120$ and $6 \times 6 = 36$ Find halves of even numbers to 200 and beyond using partitioning Begin to halve amounts of money e.g. half of $\pounds 52.40$ is $\pounds 26.20$</p>	<p>Use a written method to divide a 2-digit or a 3-digit number by a 1-digit number Give remainders as whole numbers Begin to reduce fractions to their simplest forms Find unit and non-unit fractions of larger amounts</p>	<p>Know by heart all the division facts up to $100 \div 10$ Divide whole numbers by 10 and 100 to give whole number answers or answers with 1 decimal place Perform divisions just above the 10th multiple using the written layout and understanding how to give a remainder as a whole number Find unit fractions of amounts</p>

UPPER KEY STAGE 2

Children move on from dealing mainly with whole numbers to performing arithmetic operations with both decimals and fractions.

Addition and subtraction: Children will consolidate their use of written procedures in adding and subtracting whole numbers with up to 6 digits and also decimal numbers with up to 2 decimal places. Mental strategies for adding and subtracting increasingly large numbers will also be taught. These will draw upon children's robust understanding of place value and knowledge of number facts. Negative numbers will be added and subtracted.

Multiplication and division: Efficient and flexible strategies for mental multiplication and division are taught and practised, so that children can perform appropriate calculations even when the numbers are large, such as $40\,000 \times 6$ or $40\,000 \div 8$. In addition, it is in Years 5 and 6 that children extend their knowledge and confidence in using written algorithms for multiplication and division.

Fractions, decimals, percentages and ratio: Fractions and decimals are also added, subtracted, divided and multiplied, within the bounds of children's understanding of these more complicated numbers. Children will also calculate simple percentages and ratios.

Year 5

	Mental calculation	Written calculation	Default for ALL children
Y5 +	<p>Know number bonds to 1 and to the next whole number</p> <p>Add to the next 10 from a decimal number e.g. $13.6 + 6.4 = 20$</p> <p>Add numbers with 2 significant digits only, using mental strategies e.g. $3.4 + 4.8$ e.g. $23\,000 + 47\,000$</p> <p>Add 1- or 2-digit multiples of 10, 100, 1000, 10 000 and 100 000 e.g. $8000 + 7000$ e.g. $600\,000 + 700\,000$</p> <p>Add near multiples of 10, 100, 1000, 10 000 and 100 000 to other numbers e.g. $82\,472 + 30\,004$</p> <p>Add decimal numbers which are near multiples of 1 or 10, including money e.g. $6.34 + 1.99$ e.g. $\pounds 34.59 + \pounds 19.95$</p> <p>Use place value and number facts to add two or more 'friendly' numbers, including money and decimals e.g. $3 + 8 + 6 + 4 + 7$ e.g. $0.6 + 0.7 + 0.4$ e.g. $2056 + 44$</p>	<p>Use column addition to add two or three whole numbers with up to 5 digits</p> <p>Use column addition to add any pair of 2-place decimal numbers, including amounts of money</p> <p>Begin to add related fractions using equivalences e.g. $\frac{1}{2} + \frac{1}{6} = \frac{3}{6} + \frac{1}{6}$</p> <p>Choose the most efficient method in any given situation</p>	<p>Add numbers with only 2 digits which are not zeros e.g. $3.4 + 5.8$</p> <p>Derive swiftly and without any difficulty number bonds to 100</p> <p>Add 'friendly' large numbers using knowledge of place value and number facts</p> <p>Use expanded column addition to add pairs of 4- and 5-digit numbers</p>

Y5

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Subtract numbers with 2 significant digits only, using mental strategies

e.g. $6.2 - 4.5$

e.g. $72\,000 - 47\,000$

Subtract 1- or 2-digit multiples of 10, 100, 1000, 10 000 and 100 000

e.g. $8000 - 3000$

e.g. $60\,000 - 200\,000$

Subtract 1- or 2-digit near multiples of 10, 100, 1000, 10 000 and 100 000 from other numbers

e.g. $82\,472 - 30\,004$

Subtract decimal numbers which are near multiples of 1 or 10, including money

e.g. $6.34 - 1.99$

e.g. $£34.59 - £19.95$

Use counting up subtraction, with knowledge of number bonds to 10, 100 or £1, as a strategy to perform mental subtraction

e.g. $£10 - £3.45$

e.g. $1000 - 782$

Recognise fraction complements to 1 and to the next whole number

e.g. $1\frac{2}{5} + \frac{3}{5} = 2$

Use compact or expanded column subtraction to subtract numbers with up to 5 digits

Use complementary addition for subtractions where the larger number is a multiple or near multiple of 1000

Use complementary addition for subtractions of decimal numbers with up to 2 places, including amounts of money

Begin to subtract related fractions using equivalences

e.g. $\frac{1}{2} - \frac{1}{6} = \frac{2}{6}$

Choose the most efficient method in any given situation

Derive swiftly and without difficulty number bonds to 100

Use counting up with confidence to solve most subtractions, including finding complements to multiples of 1000

e.g. $3000 - 2387$

<p>Y5 ×</p>	<p>Know by heart all the multiplication facts up to 12×12 Multiply whole numbers and 1- and 2-place decimals by 10, 100, 1000, 10 000 Use knowledge of factors and multiples in multiplication <i>e.g. 43×6 is double 43×3</i> <i>e.g. 28×50 is $\frac{1}{--2}$ of $28 \times 100 = 1400$</i> Use knowledge of place value and rounding in mental multiplication <i>e.g. 67×199 as $67 \times 200 - 67$</i> Use doubling and halving as a strategy in mental multiplication <i>e.g. 58×5 is half of 58×10</i> <i>e.g. 34×4 is 34 doubled twice</i> Partition 2-digit numbers, including decimals, to multiply by a 1-digit number mentally <i>e.g. 6×27 as 6×20 (120) plus 6×7 (42)</i> <i>e.g. 6.3×7 as 6×7 (42) plus 0.3×7 (2.1)</i> Double amounts of money by partitioning <i>e.g. $\pounds 37.45$ doubled is $\pounds 37$ doubled ($\pounds 74$) plus 45p doubled (90p) giving a total of $\pounds 74.90$</i></p>	<p>Use short multiplication to multiply a 1-digit number by a number with up to 4 digits Use long multiplication to multiply 3-digit and 4-digit numbers by a number between 11 and 20 Choose the most efficient method in any given situation Find simple percentages of amounts <i>e.g. 10%, 5%, 20%, 15% and 50%</i> Begin to multiply fractions and mixed numbers by whole numbers ≤ 10 <i>e.g. $4 \times \frac{2}{3} = \frac{8}{3} = 2 \frac{2}{3}$</i></p>	<p>Know multiplication tables to 11×11 Multiply whole numbers and 1-place decimals by 10, 100 and 1000 Use knowledge of factors as aids to mental multiplication <i>e.g. 13×6 is double 13×3</i> <i>e.g. 23×5 is $\frac{1}{--2}$ of 23×10</i> Use the grid method to multiply numbers with up to 4 digits by 1-digit numbers Use the grid method to multiply 2-digit numbers by 2-digit numbers</p>
<p>Y5 ÷</p>	<p>Know by heart all the division facts up to $144 \div 12$ Divide whole numbers by 10, 100, 1000, 10 000 to give whole number answers or answers with 1, 2 or 3 decimal places Use doubling and halving as mental division strategies <i>e.g. $34 \div 5$ is $(34 \div 10) \times 2$</i> Use knowledge of multiples and factors, as well as tests for divisibility, in mental division <i>e.g. $246 \div 6$ is $123 \div 3$</i> <i>e.g. We know that 525 divides by 25 and by 3</i> Halve amounts of money by partitioning <i>e.g. $\frac{1}{2}$ of $\pounds 75.40 = \frac{1}{2}$ of $\pounds 75$ ($\pounds 37.50$) plus half of 40p (20p) which is $\pounds 37.70$</i> Divide larger numbers mentally by subtracting the 10th or 100th multiple as appropriate <i>e.g. $96 \div 6$ is $10 + 6$, as $10 \times 6 = 60$ and $6 \times 6 = 36$</i> <i>e.g. $312 \div 3$ is $100 + 4$ as $100 \times 3 = 300$ and $4 \times 3 = 12$</i> Know tests for divisibility by 2, 3, 4, 5, 6, 9 and 25 Know square numbers and cube numbers Reduce fractions to their simplest form</p>	<p>Use short division to divide a number with up to 4 digits by a number ≤ 12 Give remainders as whole numbers or as fractions Find non-unit fractions of large amounts Turn improper fractions into mixed numbers and vice versa Choose the most efficient method in any given situation</p>	<p>Know by heart division facts up to $121 \div 11$ Divide whole numbers by 10, 100 or 1000 to give answers with up to 1 decimal place Use doubling and halving as mental division strategies Use an efficient written method to divide numbers ≤ 1000 by 1-digit numbers Find unit fractions of 2- and 3-digit numbers</p>

Year 6

	Mental calculation	Written calculation	Default for ALL children
Y6 +	<p>Know by heart number bonds to 100 and use these to derive related facts e.g. $3 \cdot 46 + 0 \cdot 54$</p> <p>Derive, quickly and without difficulty, number bonds to 1000</p> <p>Add small and large whole numbers where the use of place value or number facts makes the calculation do-able mentally e.g. $34\ 000 + 8000$</p> <p>Add multiples of powers of 10 and near multiples of the same e.g. $6345 + 199$</p> <p>Add negative numbers in a context such as temperature where the numbers make sense</p> <p>Add two 1-place decimal numbers or two 2-place decimal numbers less than 1 e.g. $4 \cdot 5 + 6 \cdot 3$ e.g. $0 \cdot 74 + 0 \cdot 33$</p> <p>Add positive numbers to negative numbers e.g. <i>Calculate a rise in temperature or continue a sequence beginning with a negative number</i></p>	<p>Use column addition to add numbers with up to 5 digits</p> <p>Use column addition to add decimal numbers with up to 3 decimal places</p> <p>Add mixed numbers and fractions with different denominators</p>	<p>Derive, swiftly and without difficulty, number bonds to 100</p> <p>Use place value and number facts to add 'friendly' large or decimal numbers e.g. $3 \cdot 4 + 6 \cdot 6$ e.g. $26\ 000 + 54\ 000$</p> <p>Use column addition to add numbers with up to 4-digits</p> <p>Use column addition to add pairs of 2-place decimal numbers</p>
Y6 -	<p>Use number bonds to 100 to perform mental subtraction of any pair of integers by complementary addition e.g. $1000 - 654$ as $46 + 300$ in our heads</p> <p>Use number bonds to 1 and 10 to perform mental subtraction of any pair of 1-place or 2-place decimal numbers using complementary addition and including money e.g. $10 - 3 \cdot 65$ as $0 \cdot 35 + 6$ e.g. $£50 - £34 \cdot 29$ as $71p + £15$</p> <p>Use number facts and place value to perform mental subtraction of large numbers or decimal numbers with up to 2 places e.g. $467\ 900 - 3005$ e.g. $4 \cdot 63 - 1 \cdot 02$</p> <p>Subtract multiples of powers of 10 and near multiples of the same</p> <p>Subtract negative numbers in a context such as temperature where the numbers make sense</p>	<p>Use column subtraction to subtract numbers with up to 6 digits</p> <p>Use complementary addition for subtractions where the larger number is a multiple or near multiple of 1000 or 10 000</p> <p>Use complementary addition for subtractions of decimal numbers with up to 3 places, including money</p> <p>Subtract mixed numbers and fractions with different denominators</p>	<p>Use number bonds to 100 to perform mental subtraction of numbers up to 1000 by complementary addition e.g. $1000 - 654$ as $46 + 300$ in our heads</p> <p>Use complementary addition for subtraction of integers up to 10 000 e.g. $2504 - 1878$</p> <p>Use complementary addition for subtractions of 1-place decimal numbers and amounts of money e.g. $£7 \cdot 30 - £3 \cdot 55$</p>

<p>Y6 ×</p>	<p>Know by heart all the multiplication facts up to 12×12 Multiply whole numbers and decimals with up to 3 places by 10, 100 or 1000 e.g. $234 \times 1000 = 234\ 000$ e.g. $0.23 \times 1000 = 230$ Identify common factors, common multiples and prime numbers and use factors in mental multiplication e.g. 326×6 is 652×3 which is 1956 Use place value and number facts in mental multiplication e.g. $4000 \times 6 = 24\ 000$ e.g. $0.03 \times 6 = 0.18$ Use doubling and halving as mental multiplication strategies, including to multiply by 2, 4, 8, 5, 20, 50 and 25 e.g. 28×25 is a quarter of $28 \times 100 = 700$ Use rounding in mental multiplication e.g. 34×19 as $(34 \times 20) - 34$ Multiply 1- and 2-place decimals by numbers up to and including 10 using place value and partitioning e.g. 3.6×4 is $12 + 2.4$ e.g. 2.53×3 is $6 + 1.5 + 0.09$ Double decimal numbers with up to 2 places using partitioning e.g. 36.73 doubled is double 36 (72) plus double 0.73 (1.46)</p>	<p>Use short multiplication to multiply a 1-digit number by a number with up to 4 digits Use long multiplication to multiply a 2-digit number by a number with up to 4 digits Use short multiplication to multiply a 1-digit number by a number with 1 or 2 decimal places, including amounts of money Multiply fractions and mixed numbers by whole numbers Multiply fractions by proper fractions Use percentages for comparison and calculate simple percentages</p>	<p>Know by heart all the multiplication facts up to 12×12 Multiply whole numbers and 1- and 2-place decimals by 10, 100 and 1000 Use an efficient written method to multiply a 1-digit or a teen number by a number with up to 4 digits by partitioning (grid method) Multiply a 1-place decimal number up to 10 by a number ≤ 100 using the grid method</p>
<p>Y6 ÷</p>	<p>Know by heart all the division facts up to $144 \div 12$ Divide whole numbers by powers of 10 to give whole number answers or answers with up to 3 decimal places Identify common factors, common multiples and primes numbers and use factors in mental division e.g. $438 \div 6$ is $219 \div 3$ which is 73 Use tests for divisibility to aid mental calculation Use doubling and halving as mental division strategies, for example to divide by 2, 4, 8, 5, 20 and 25 e.g. $628 \div 8$ is halved three times: $314, 157, 78.5$ Divide 1- & 2-place decimals by numbers up to and including 10 using place value e.g. $2.4 \div 6 = 0.4$ e.g. $0.65 \div 5 = 0.13$ e.g. $\pounds 6.33 \div 3 = \pounds 2.11$ Halve decimal numbers with up to 2 places using partitioning e.g. Half of 36.86 is half of 36 (18) plus half of 0.86 (0.43) Know and use equivalence between simple fractions, decimals and percentages, including in different contexts Recognise a given ratio and reduce a given ratio to its lowest terms</p>	<p>Use short division to divide a number with up to 4 digits by a 1-digit or a 2-digit number Use long division to divide 3-digit and 4-digit numbers by 'friendly' 2-digit numbers Give remainders as whole numbers or as fractions or as decimals Divide a 1-place or a 2-place decimal number by a number ≤ 12 using multiples of the divisors Divide proper fractions by whole numbers</p>	<p>Know by heart all the division facts up to $144 \div 12$ Divide whole numbers by 10, 100, 1000 to give whole number answers or answers with up to 2 decimal places Use an efficient written method, involving subtracting powers of 10 times the divisor, to divide any number of up to 1000 by a number ≤ 12 e.g. $836 \div 11$ as $836 - 770$ (70×11) leaving 66 which is 6×11, giving the answer 76 Divide a 1-place decimal by a number ≤ 10 using place value and knowledge of division facts</p>